

# FLS 6441 - Methods III: Explanation and Causation

Week 2 - A Framework for Explanation

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Explanation

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Causal Inference

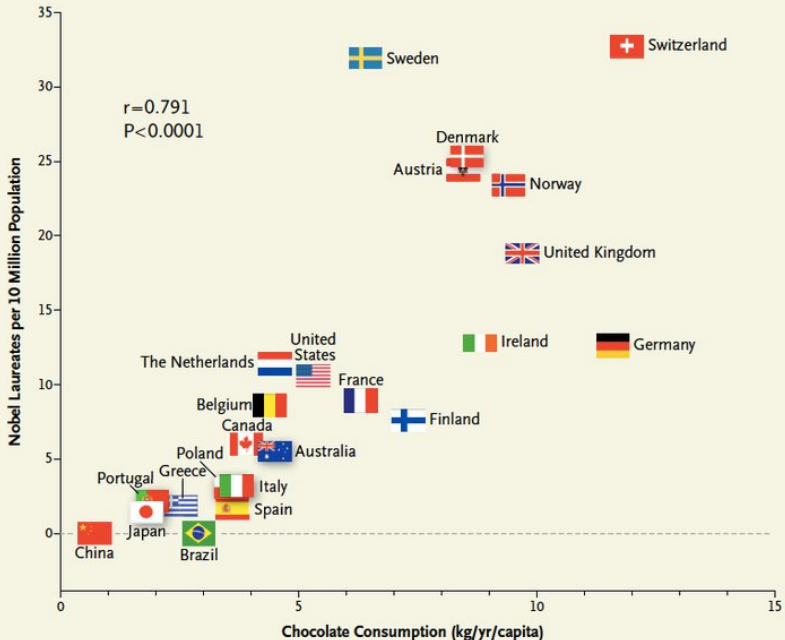
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Why Observational Data is Biased

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Rest of the Course

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  - ▶ But for **intervention**, correlation does not help: forcing people to eat more chocolate does nothing on its own to produce more Nobel Laureates
  - ▶ For **explanation**, correlation also fails - it is no *explanation* to say that Switzerland has the most Nobel Laureates because it has the highest chocolate consumption







## Explanation

- ▶ What does it mean to explain something?
- ▶ To give an account of what happens, *and why*
  - ▶ The 'chain of causation'
- ▶ If  $D$  explains  $y$ , we are saying that the *absence* of  $D$  would have led to a different value of  $y$

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- ▶ There exists a 'counterfactual' possibility that did not happen

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### Probabilistic Explanation

- ▶ If  $D$  happens, the **probability** of  $Y$  increases
- ▶ Treatment effects are a distribution, not a single value

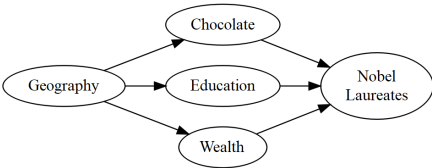
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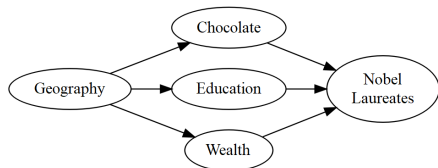
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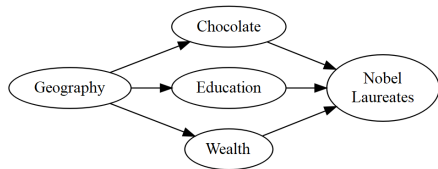
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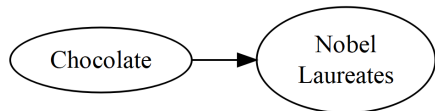
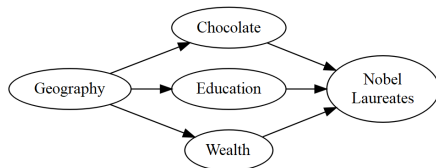
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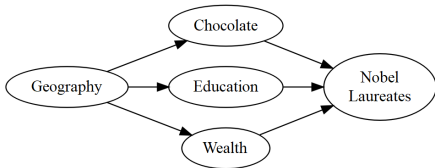


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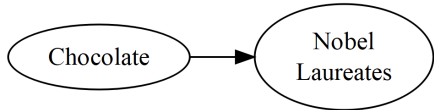


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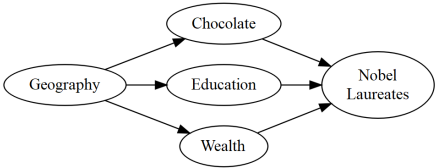


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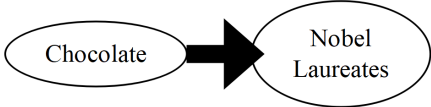


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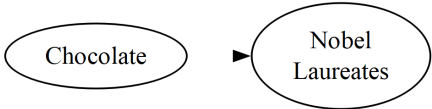
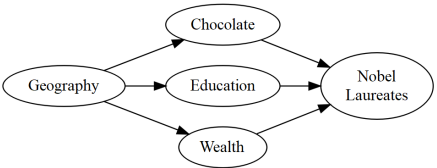
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- ▶ AND to clearly define a '**Control**'
  - ▶ What is the opposite of investing \$1bn in education?
  - ▶ No investment, or investing it elsewhere?
- ▶ Define treatment:

$$D_i = \begin{cases} 1, & \text{if treated} \\ 0, & \text{if not treated} \end{cases}$$

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  - ▶ All outcomes are **probabilistic** (due to all the other factors we haven't accounted for)
  - ▶ If we study 20 outcomes, on average one will show a significant effect even with no real causal effect
- ▶ So we usually want to study a **single outcome**



# Causal Inference

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$$Y_{Di} = \begin{cases} Y_{1i} & \text{Potential Outcome if unit } i \text{ treated} \\ Y_{0i} & \text{Potential Outcome if unit } i \text{ NOT treated} \end{cases}$$

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Rest of the Course

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## Causal Inference

Potential Outcomes are just another Variable for each Unit

	GDP Growth if Democracy	GDP Growth if NOT Democ- racy	Treatment Effect
	$Y_1$	$Y_0$	$Y_1 - Y_0$
Brasil	6	3	3
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$$ATE = E(\alpha_i) = E(Y_1 - Y_0) = E(Y_1) - E(Y_0) = \frac{\sum_i (Y_{1i} - Y_{0i})}{N}$$

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<b>Average Treatment Effect</b>	<b>4.17</b>	<b>3.17</b>	<b>1</b>

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### Average Treatment Effect on the Treated

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$$ATU = E(\alpha_i | D = 0) = E(Y_1 - Y_0 | D = 0) = \frac{\sum_i (Y_{1i} - Y_{0i} | D = 0)}{N_{Control}} \quad (2)$$

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- ▶ The three effect estimates are usually different
  - ▶ The effect democracy has had in Europe is different to the effect if it were introduced in Africa

## Causal Inference

## Potential Outcomes Example

	Democracy?	GDP Growth if Democracy	GDP Growth if NOT Democracy	<b>Treatment Effect</b>
	$D_i$	$Y_1$	$Y_0$	$Y_1 - Y_0$
Brasil	0	6	3	3
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Bolivia	1	0	2	-2
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$$Y_i^{obs} = \begin{cases} Y_{1i} & \text{if } D_i = 1 \\ Y_{0i} & \text{if } D_i = 0 \end{cases}$$

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# Causal Inference

What we see in our Data:

	Democracy?	<b>Observed</b> GDP Growth
	$D_i$	$\gamma^{obs}$
Brasil	0	3
Argentina	0	5
Uruguay	0	3
Bolivia	1	0
Colombia	1	4
Peru	0	2

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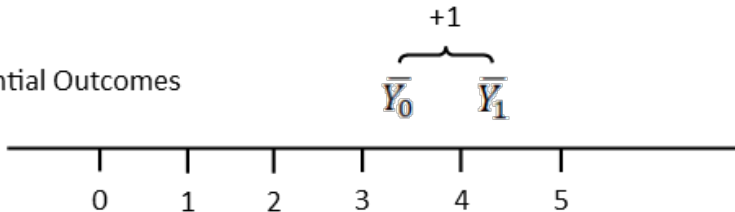
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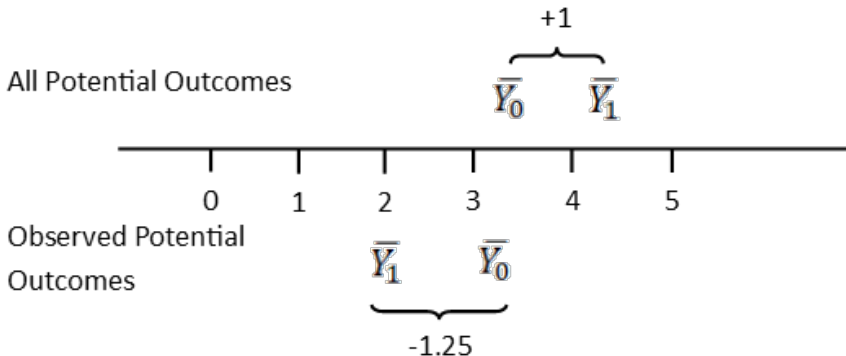
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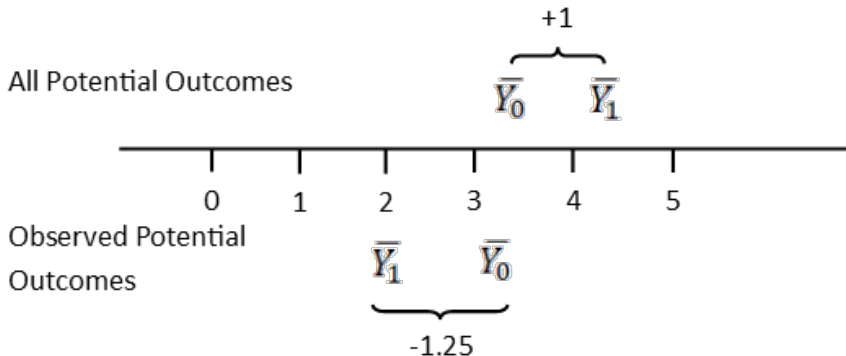
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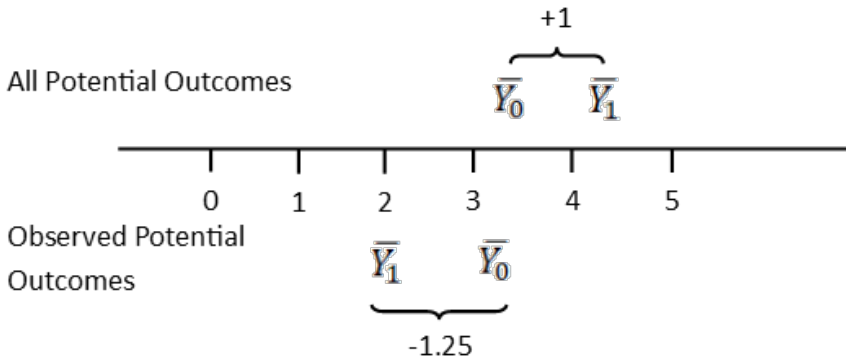
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- ▶  $E(Y_0)$  values are **biased higher** in the observed data

## Causal Inference

- ▶ **So what went wrong?**
- ▶ The potential outcomes we **observe** are a **biased representation** of the potential outcomes of all the units



- ▶  $E(Y_1)$  values are **biased lower** in the observed data
- ▶  $E(Y_0)$  values are **biased higher** in the observed data
- ▶ So  $E(Y_1) - E(Y_0)$  is **biased**

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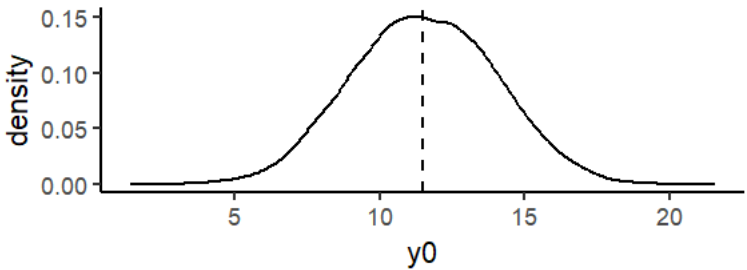
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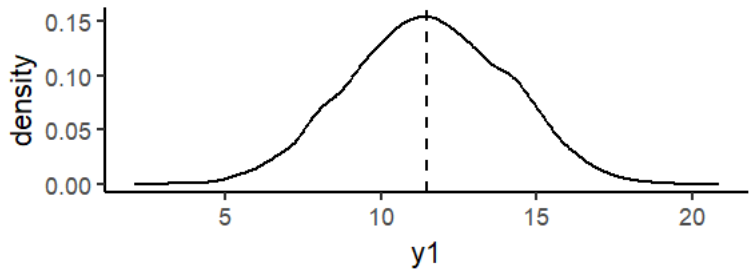
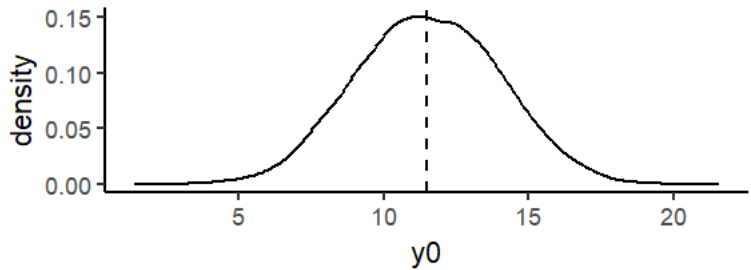
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  - ▶ Causal effects are **biased**

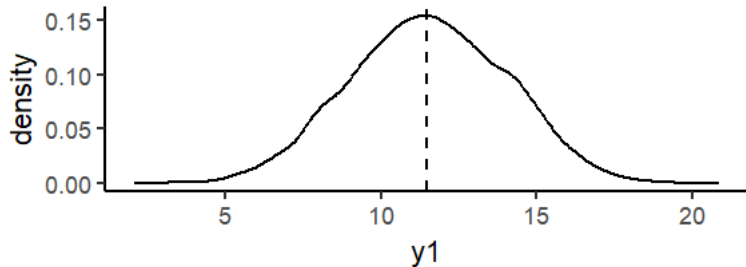
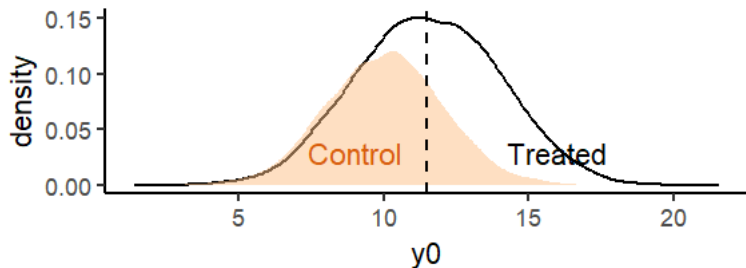
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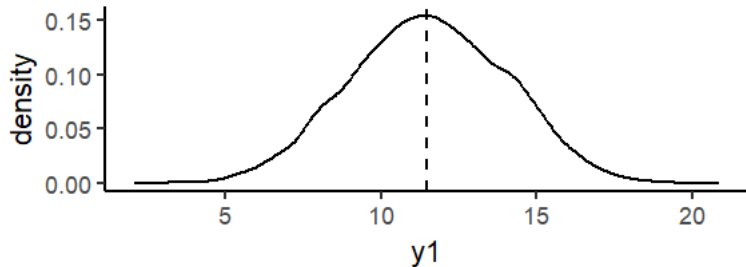
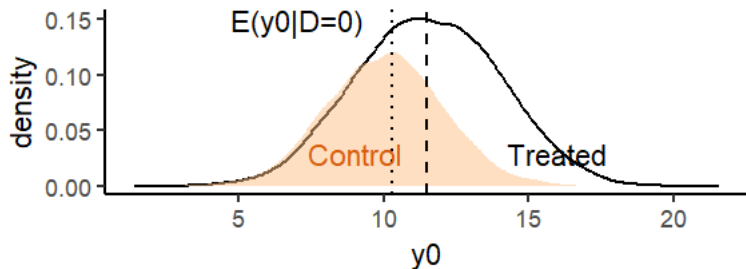


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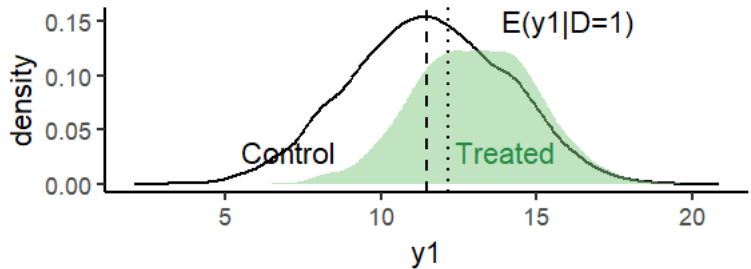
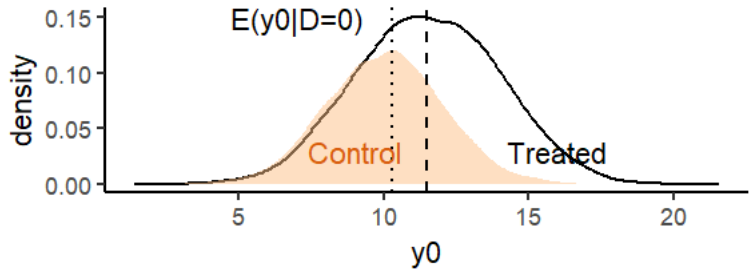




## Causal Inference



# Causal Inference



# Causal Inference

- ▶ Lots of averages:

		Hypothetical outcome	
		$Y_0$	$Y_1$
Actual Treatment	$D = 0$	$E(Y_{0i} D = 0)$	$E(Y_{1i} D = 0)$
	$D = 1$	$E(Y_{0i} D = 1)$	$E(Y_{1i} D = 1)$

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	No Average Effect $E(Y_1 - Y_0) = 0$	"Sharp null": No individual effects $(Y_{1i} - Y_{0i} = 0)$
Brasil	2	0
Argentina	3	0
Uruguay	0	0
Bolivia	-2	0
Colombia	0	0
Peru	-3	0
<b>Average</b>	<b>0</b>	<b>0</b>

## Exercise

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  - ▶ Label this number  $Y_0$ .
- ▶ These are your **potential outcomes**.

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- ▶ Now we will consider how estimates of the average effect of fruit on happiness vary depending on how apples are distributed:
  1. All the female participants are given an apple.
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  3. You are free to choose yourself to take an apple or not.
  4. Apples are distributed randomly



## Bias

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  1. Omitted Variables



# Bias

- ▶ Why are potential outcomes biased in our data?
  1. Omitted Variables
  2. Reverse Causation
  3. Selection Bias





## Bias

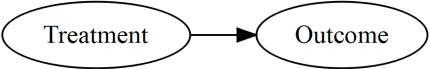
- ▶ Why are potential outcomes biased in our data?
  1. Omitted Variables
  2. Reverse Causation
  3. Selection Bias
- ▶ In all of these cases **the potential outcomes are distorted**
- ▶ They are **not independent of treatment assignment**



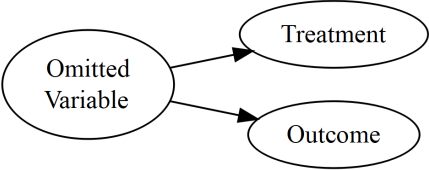


# Omitted Variable Bias

A real causal relationship:

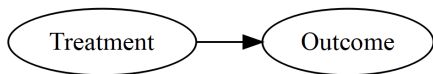


Being misled by omitted variable bias:

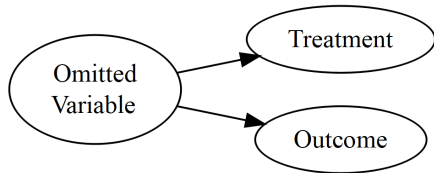


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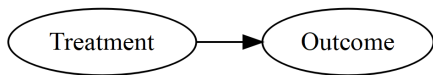
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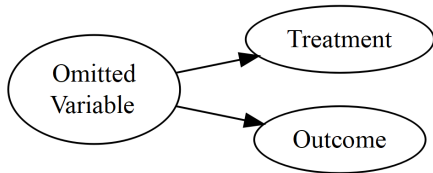
- ▶ A third variable causes some units to have **different values of potential outcomes**, AND for those **same units to be treated**

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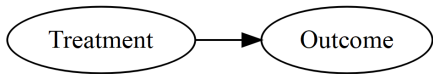
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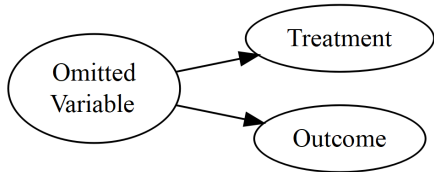
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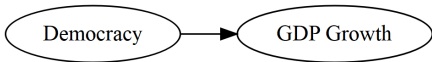
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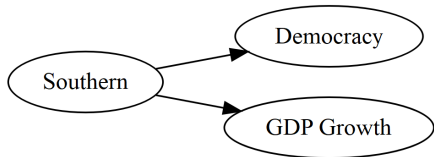
- ▶ A third variable causes some units to have **different values of potential outcomes**, AND for those **same units to be treated**
- ▶ So treated units have non-representative  $Y_1$
- ▶ And control units have non-representative  $Y_0$

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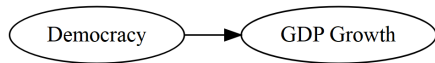
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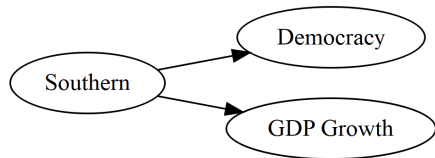


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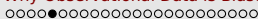
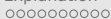
A real causal relationship:



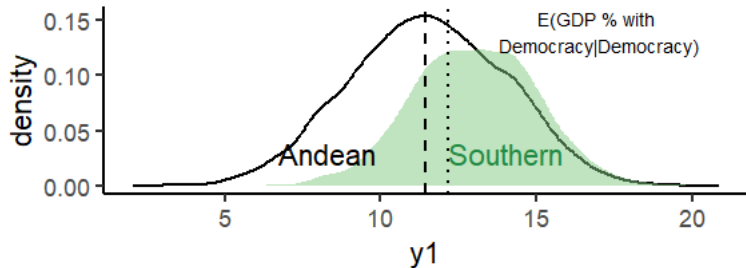
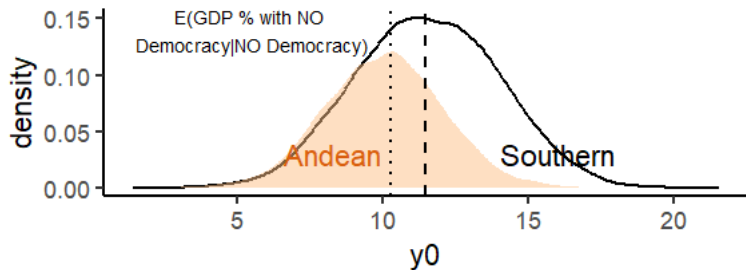
Being misled by omitted variable bias:



- ▶ Southern Cone countries faced conditions that encouraged both democracy and rapid GDP growth



## Omitted Variable Bias

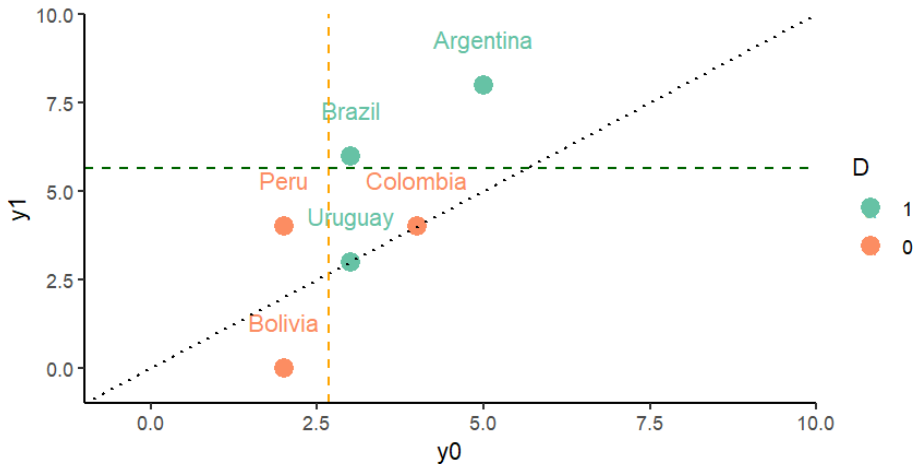


## Omitted Variable Bias

	Andean?	Democracy?	GDP Growth if Dem	GDP Growth if NOT Dem	Treatment Effect
	$X_i$	$D_i$	$Y_1$	$Y_0$	$Y_1 - Y_0$
Brasil	1	1	6	?	?
Argentina	1	1	8	?	?
Uruguay	1	1	3	?	?
Bolivia	0	0	?	2	?
Colombia	0	0	?	4	?
Peru	0	0	?	2	?
<b>Average Treatment Effect</b>			<b>5.7</b>	<b>2.7</b>	<b>3</b>



## Omitted Variable Bias



►  $E(Y_1|D = 1) - E(Y_0|D = 0) = 5.7 - 2.7 = 3$



## Omitted Variable Bias

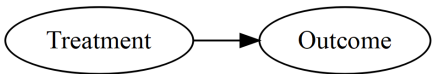
- ▶ Let's say that  $Y_{1i} = Y_{0i} + \alpha$ , where  $\alpha$  is the real constant treatment effect

$$\hat{ATE} = E(Y_1|D = 1) - E(Y_0|D = 0)$$

$$\hat{ATE} = \underbrace{\alpha}_{\text{Real ATE}} + \underbrace{E(Y_0|D = 1) - E(Y_0|D = 0)}_{\text{Bias}}$$

# Reverse Causation

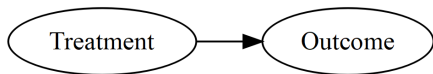
A real causal relationship:



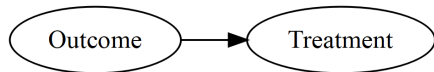


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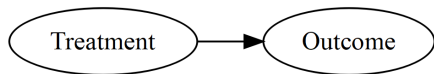


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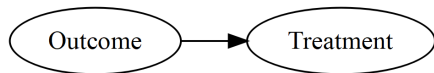


## Reverse Causation

A real causal relationship:



Being misled by reverse causation:



- ▶  $D$  does not affect  $Y$ , but higher  $Y$  makes treatment ( $D$ ) more likely

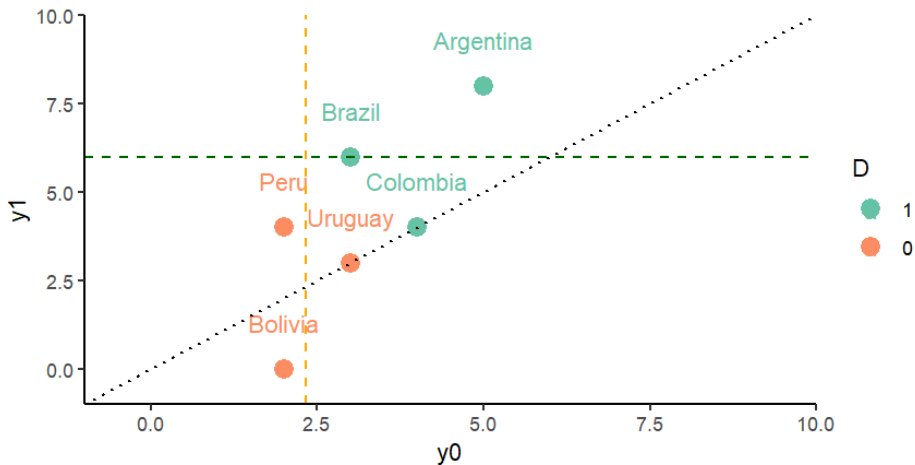








# Reverse Causation



$$\blacktriangleright E(Y_1|D=1) - E(Y_0|D=0) = 6 - 2.3 = 3.7$$

# Causal Inference

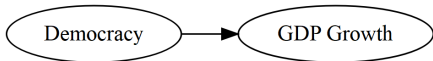
	Democracy?	GDP Growth if Dem	GDP Growth if NOT Dem	Treatment Effect
	$D_i$	$Y_1$	$Y_0$	$Y_1 - Y_0$
Brasil	1	6	?	?
Argentina	1	8	?	?
Uruguay	0	?	3	?
Bolivia	0	?	2	?
Colombia	1	4	?	?
Peru	0	?	2	?
<b>Average Treatment Effect</b>		<b>6</b>	<b>2.3</b>	<b>3.7</b>



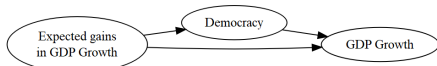


# Selection Bias

A real causal relationship:

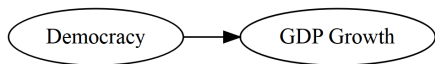


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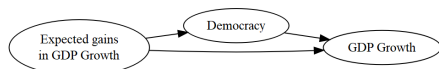


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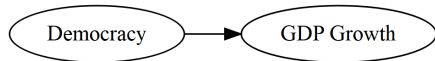
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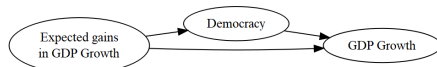
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Being misled by Selection Bias:

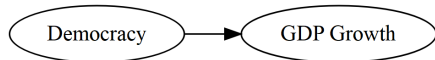


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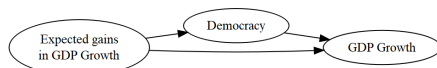


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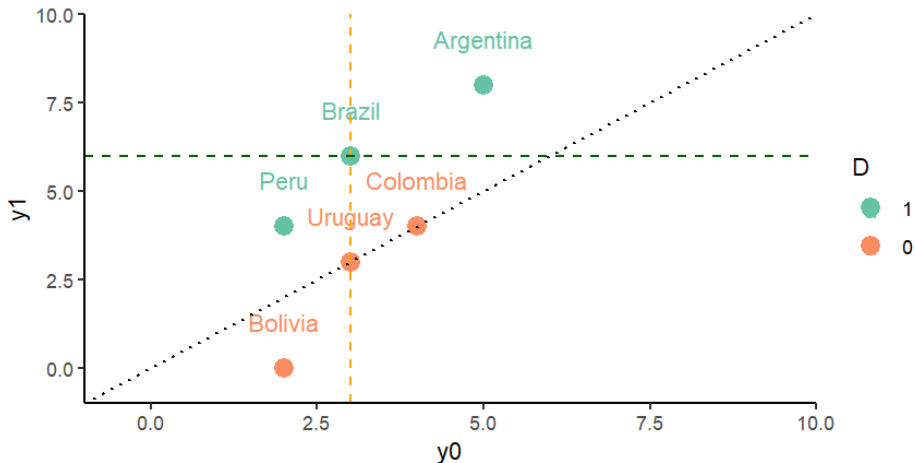


- ▶ The units which benefit most from treatment (largest  $y_1 - y_0$ ) **choose treatment**
- ▶ We don't see any of the low  $y_1$ 's of units which avoid treatment
  - ▶ Countries which can boost their GDP growth by becoming a democracy choose to democratize
  - ▶ Ex. Mexico? Myanmar?

## Self-Selection Bias

	Democracy?	GDP Growth if Dem	GDP Growth if NOT Dem	<b>Treatment Effect</b>
	$D_i$	$Y_1$	$Y_0$	$Y_1 - Y_0$
Brasil	1	6	?	?
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Uruguay	0	?	3	?
Bolivia	0	?	2	?
Colombia	0	?	4	?
Peru	1	4	?	?
<b>Average Treat- ment Effect</b>		<b>6</b>	<b>3</b>	<b>3</b>

## Self-Selection Bias



►  $E(y_1|D = 1) - E(y_0|D = 0) = 6 - 3 = 3$



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$$\underbrace{E(Y_i|D=1) - E(Y_i|D=0)}_{\text{Observed Effect}} = \underbrace{E(Y_{1i} - Y_{0i})}_{\text{Real ATE}}$$

Observed Effect

Real ATE

$$+ \underbrace{\frac{1}{2} [E(Y_{1i}|D=1) - E(Y_{1i}|D=0)]}_{\text{Imbalance on } Y_1} + \underbrace{\frac{1}{2} [E(Y_{0i}|D=1) - E(Y_{0i}|D=0)]}_{\text{Imbalance on } Y_0}$$

(3)

NB: For equal-sized treatment and control groups









# Treatment Assignment Mechanism

- ▶ In all of these cases, **which units receive 'treatment'** ( $D_i = 1$ ), and why, affect our estimate of the relationship between  $D$  and  $Y$ 
  - ▶ This is the **Treatment Assignment Mechanism**
- ▶ Messy treatment assignment mechanisms are why basic regression is no use for explanation

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  - ▶ It means our comparison control cases are really misleading













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$$Pr(D|(Y_1, Y_0)) = Pr(D)$$

$$E(Y|D = 1) = E(Y|D = 0) = E(Y)$$







## Summary

- ▶ Template to analyze a paper:
  1. What are the treatment and outcome variables?
  2. What are the Potential Outcomes?
  3. What is the Fundamental Problem of Causal Inference in this case?
  4. How do we define the Average Treatment Effect (ATE) in this case? ATT? ATU?





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  5. What is the Treatment Assignment Mechanism?
  6. Draw a causal diagram of the variables in the study, including the treatment assignment mechanism





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  2. What are the Potential Outcomes?
  3. What is the Fundamental Problem of Causal Inference in this case?
  4. How do we define the Average Treatment Effect (ATE) in this case? ATT? ATU?
  5. What is the Treatment Assignment Mechanism?
  6. Draw a causal diagram of the variables in the study, including the treatment assignment mechanism
  7. Is Treatment Assignment independent of Potential Outcomes?
  8. Describe the risk of:
    - ▶ Omitted Variable Bias?
    - ▶ Reverse Causation?



# DOES OIL HINDER DEMOCRACY?

By MICHAEL L. ROSS\*

## INTRODUCTION

**P**OLITICAL scientists believe that oil has some very odd properties. Many studies show that when incomes rise, governments tend to become more democratic. Yet some scholars imply there is an exception to this rule: if rising incomes can be traced to a country's oil wealth, they suggest, this democratizing effect will shrink or disappear. Does oil really have antidemocratic properties? What about other minerals and other commodities? What might explain these effects?

The claim that oil and democracy do not mix is often used by area specialists to explain why the high-income states of the Arab Middle East have not become democratic. If oil is truly at fault, this insight could help explain—and perhaps, predict—the political problems of oil exporters around the world, such as Nigeria, Indonesia, Venezuela, and the oil-rich states of Central Asia. If other minerals have similar properties, this effect might help account for the absence or weakness of democracy in dozens of additional states in sub-Saharan Africa, Latin America, and Southeast Asia. Yet the "oil impedes democracy" claim has received little attention outside the circle of Mideast scholars; moreover, it has not been carefully tested with regression analysis, either within or beyond the Middle East.

I use pooled time-series cross-national data from 113 states between 1971 and 1997 to explore three aspects of the oil-impedes-democracy claim. The first is the claim's validity: is it true? Although the claim has been championed by Mideast specialists, it is difficult to test by examining only cases from the Middle East because the region provides scholars with

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# Summary

- ▶ Try experimenting with the [Causal Relationships App here](#)











## Rest of the Course

- ▶ The rest of the course is mostly about:
  - ▶ **Design-Based Solutions** to the Fundamental Problem of Causal Inference: Which treatment assignment mechanisms **avoid these biases** and provide plausible counterfactuals
  - ▶ How much can we learn with better research design?

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  - ▶ How much can we learn with better research design?
  - ▶ **Model-Based Solutions:** Not so much.

